

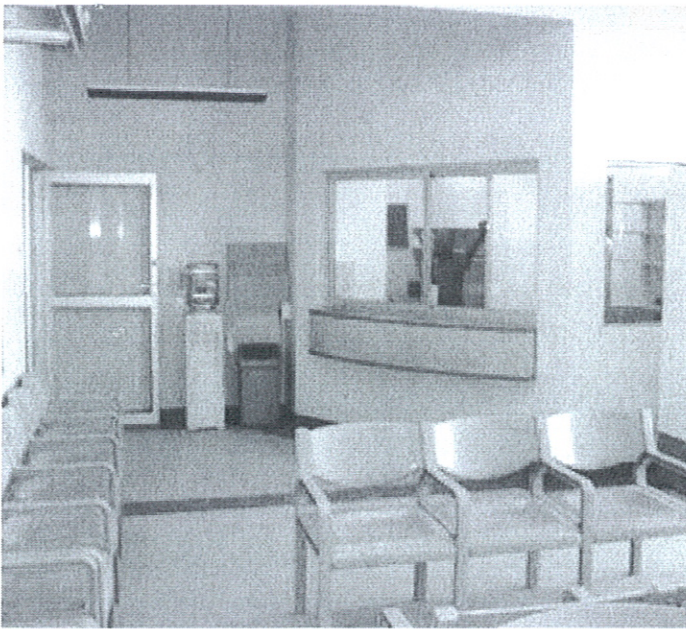
Tyler Bird

Nicole Williams .

Curtis Rasmussen

Enrique Hernandez

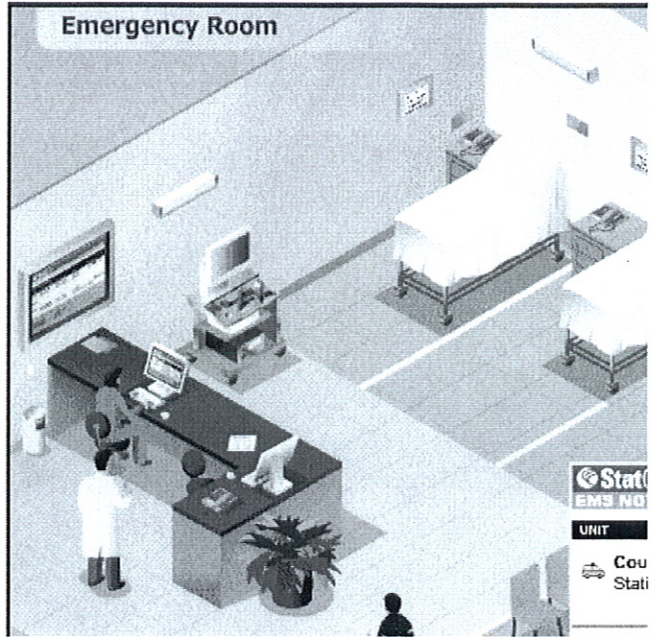
Story Board.



HERE IS A WAITING ROOM FOR AN ER

While some patients enter in through the door (control surface one) others after being treated exit through the door. THE ER IS OPERATING

AT FULL CAPACITY



Inside CV patients are treated, after treatment patients exit.



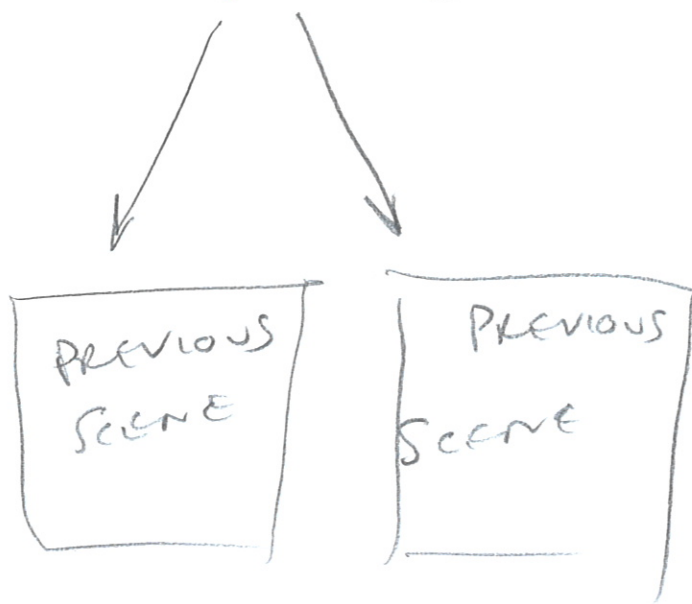
Medical Staff exchange shifts at regular intervals. They enter and exit through separate CS ( doors).

$$\Sigma M = \frac{d}{dt} \int_V \rho dV + \int_{CS} \rho \vec{V} \cdot \vec{n} dA$$



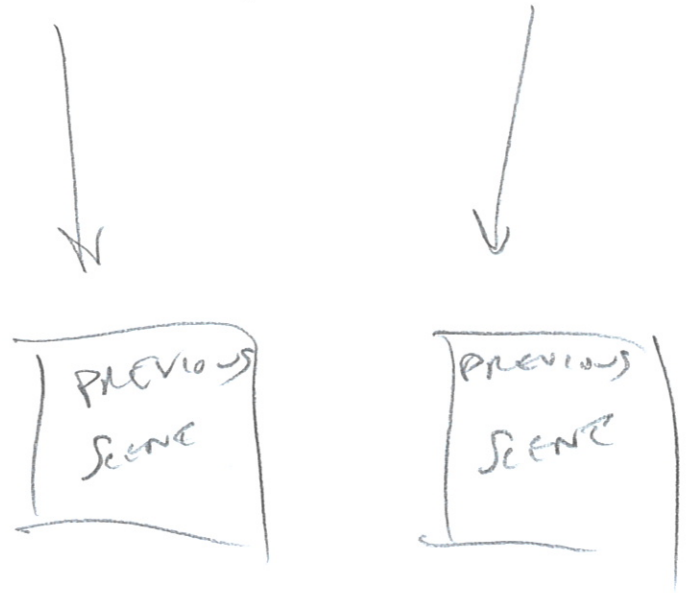
Display equation and suggest that ER is a real world model in of conservation of mass in fluids.

$$\Sigma M = \frac{\partial}{\partial t} \int_{cv} \rho dV + \int_{cs} \rho \vec{V} \cdot \vec{n} dA$$



Highlight control volume term of equation and relate to ER model (Previous footage is replayed as equation is explained).

$$\Sigma M = \frac{\partial}{\partial t} \int_{cv} \rho dV + \int_{cs} \rho \vec{V} \cdot \vec{n} dA$$



Highlight control Surface term of equation and relate to ER model (Previous footage is replayed as equation is explained, Left side also explained. )



# 1) Conservation of Mass:

Parking Lot at two time Intervals

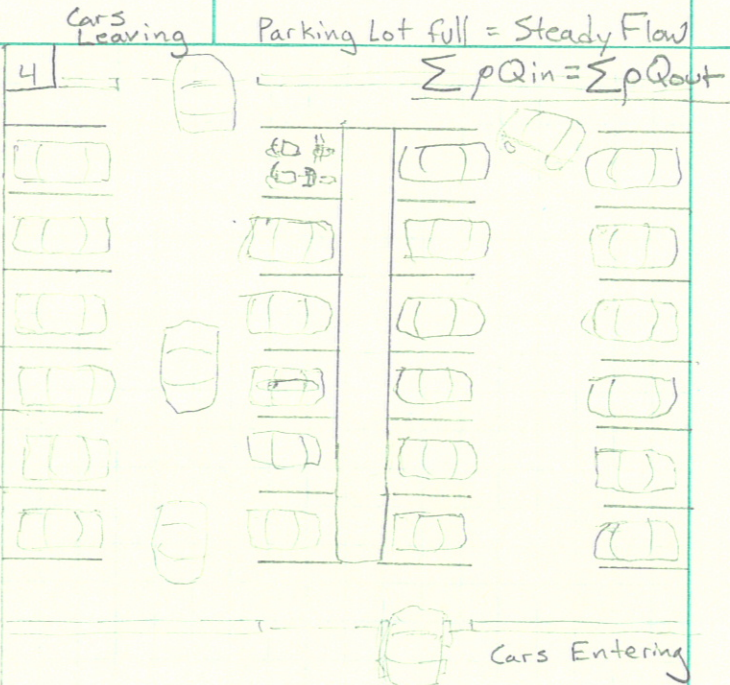
- ① Early in the morning (Empty)
- ② Late at night (Empty Again)

$$\frac{Dm}{Dt} = \frac{d}{dt} \int \rho dV + \int \rho \vec{V} \cdot \vec{n} dA$$

Change in mass of universe over change in time. This is always zero since mass is never created or destroyed

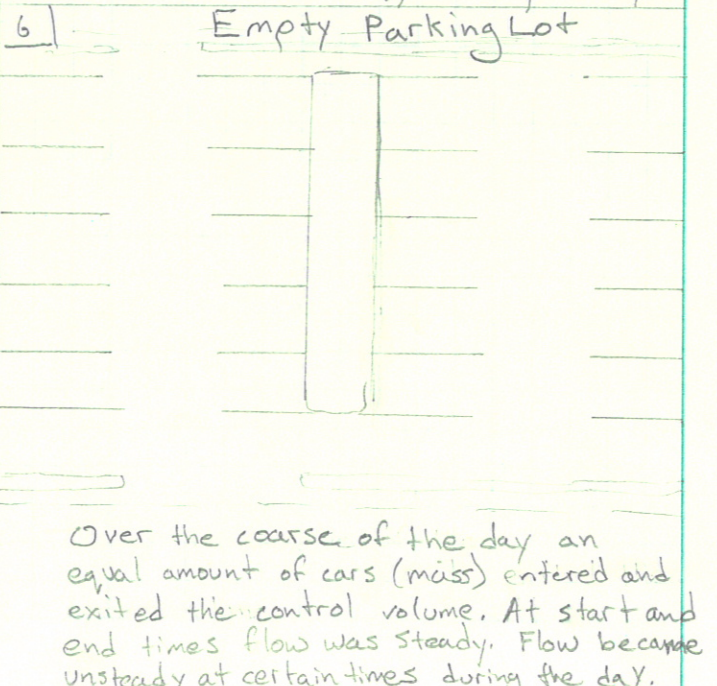
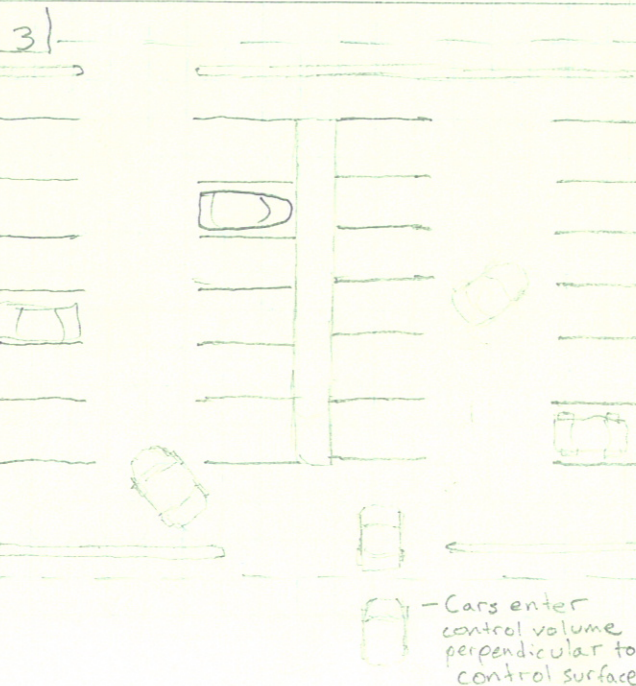
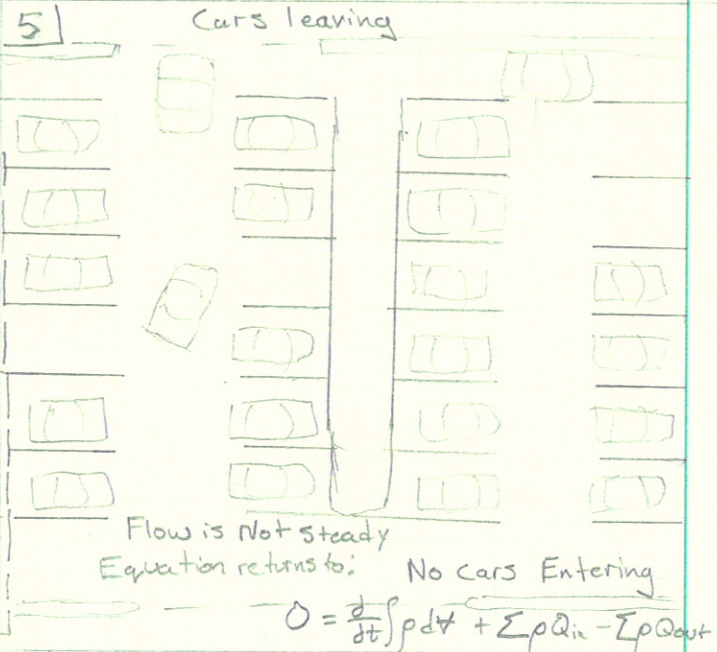
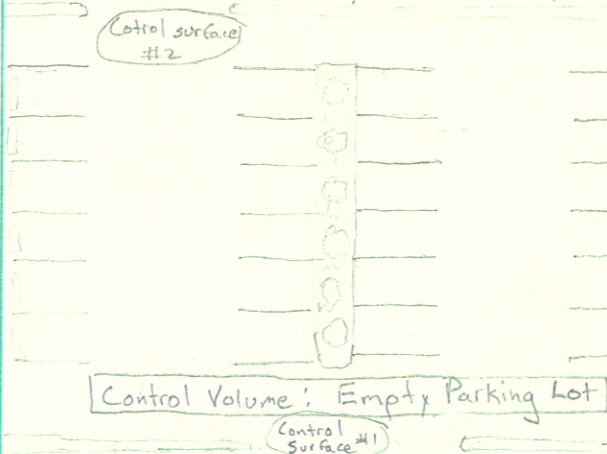
Temporal term  
This term represents the Volume and density changing with time

Spacial term  
This term represents the rate of mass in minus the rate of mass out



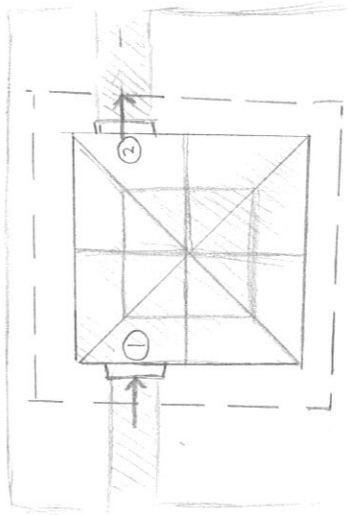
2) With a fixed control volume the above equation becomes:

$$0 = 0 + \sum \rho Q_{out} - \sum \rho Q_{in}$$



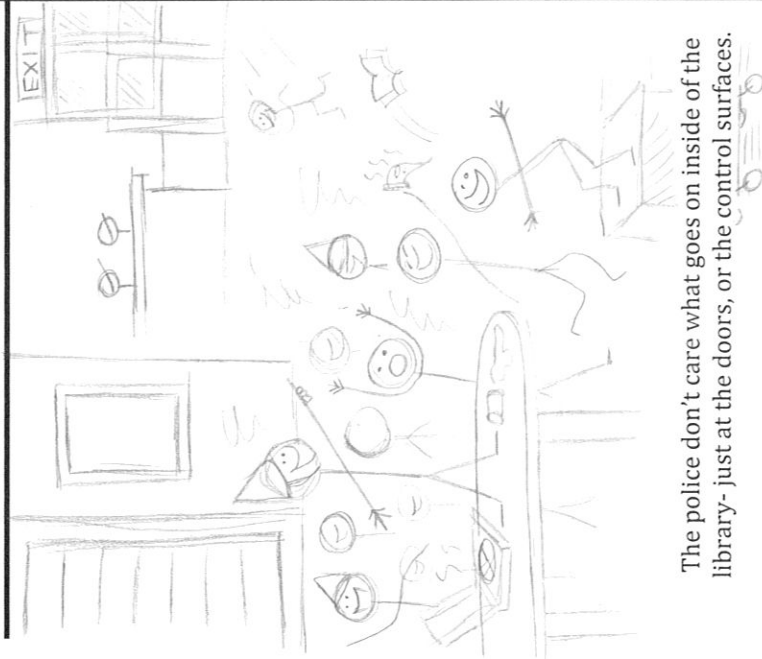


Brennon Moore  
 Hillary Ott  
 Rachelle Rosendahl

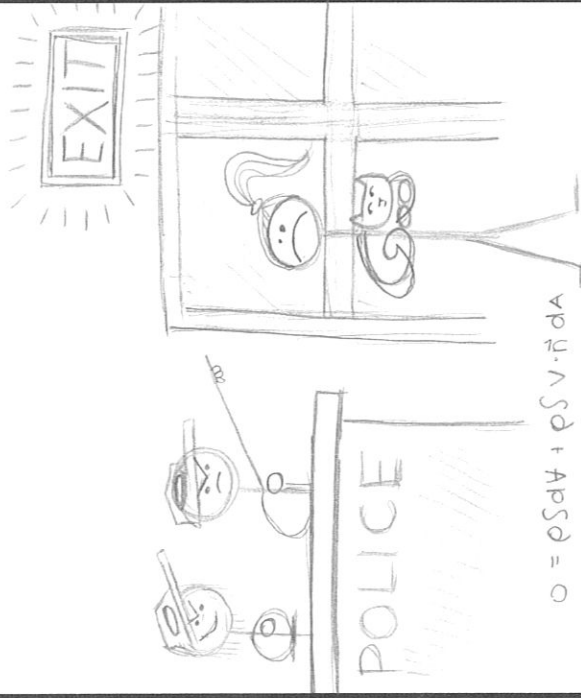


$$0 = \int \rho \mathbf{v} \cdot d\mathbf{A} + \int \rho \mathbf{v} \cdot \mathbf{n} \, dA$$

It's Finals Week at BYU, so a lot of students go to the H.B. Lee Library to study. The library acts as our control volume with the police detectors on each side as the control surfaces. Flow is unsteady because people come at different times, so the volume is changing with time.

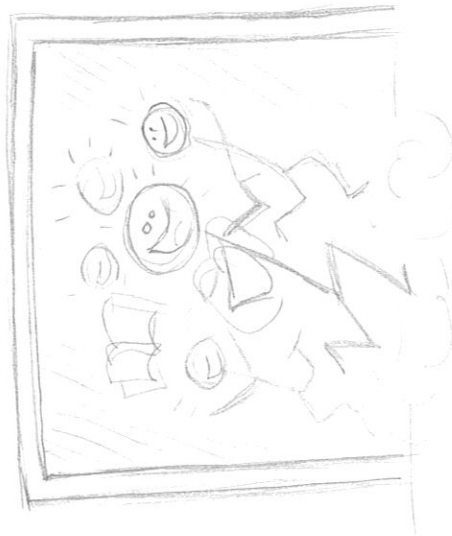


The police don't care what goes on inside of the library- just at the doors, or the control surfaces.



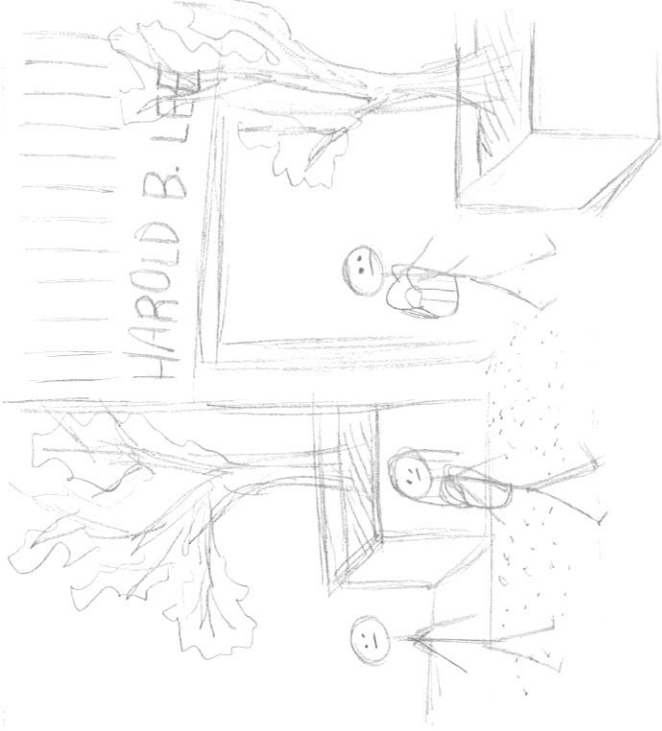
$$0 = \rho \mathbf{v} \cdot d\mathbf{A} + \rho \mathbf{v} \cdot \mathbf{n} \, dA$$

The density is constant at both control surfaces because only people are allowed in the Library.



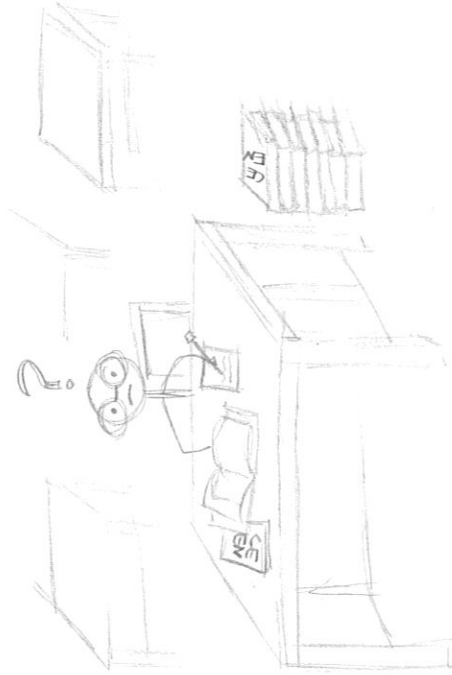
$$0 = \rho \mathbf{v} \cdot d\mathbf{A} + \sum \rho \mathbf{v}_{out} A_{out} - \sum \rho \mathbf{v}_{in} A_{in}$$

But President Monson is speaking at 2! So everyone wants to go see him speak, so there is a rush for the door. The velocity getting out is a lot faster than going in. (So velocity uniform but not constant). The area is the doors, so the area stays the same.



$$0 = \rho \mathbf{v} \cdot d\mathbf{A} + \rho \mathbf{v} \cdot \mathbf{n} \, dA$$

Students have to move in perpendicular to the detector the control surfaces.

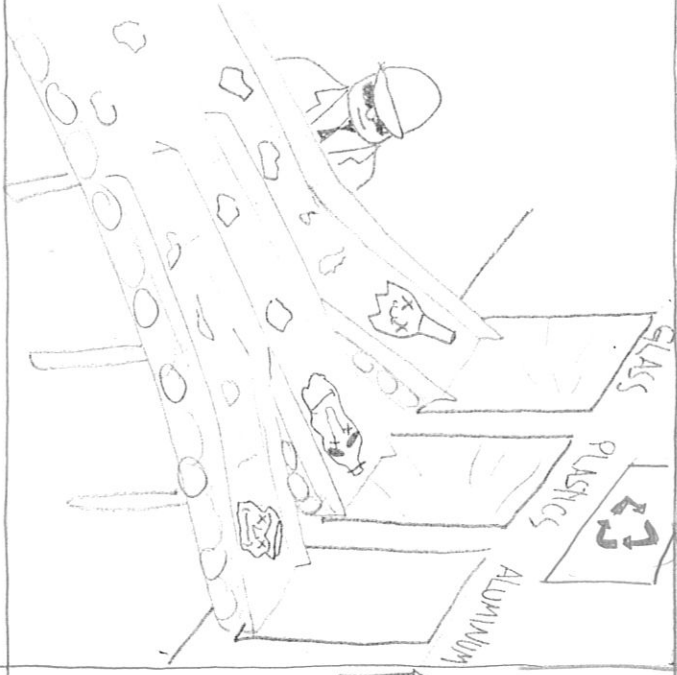


The people who went into the library = the people who exited, so mass is conserved and the left side of our equation is zero.

# CONSERVATION OF MASS a tale of three friends



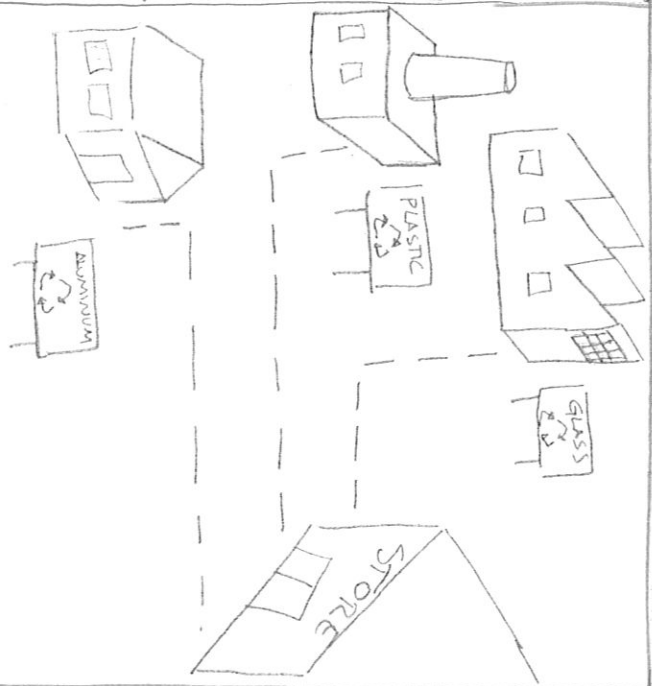
THREE FRIENDS HAVE A MEANINGFUL FACED-  
SHIP. EVER SINCE THEY JOINED THE RECYCLE  
CLUB, LIFE HAS BECOME MUCH MORE  
PEACEFUL. PRODUCT OF THEIR NEW UNDERSTANDING



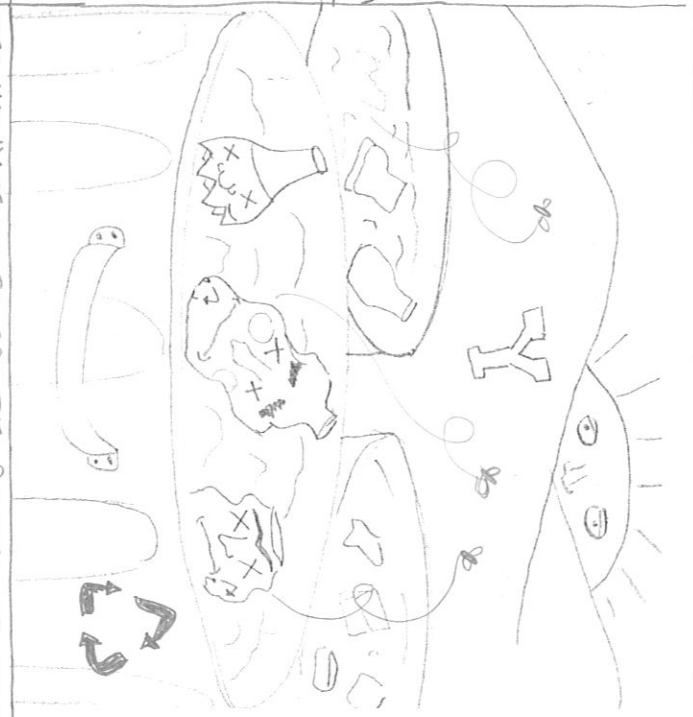
THEIR IDENTITIES REMAIN, READY TO  
BE RECOGNIZED BY THE LEARNED FEW  
WHO LOOK FOR THEIR USEFUL REMAIN.



IN THE RECYCLING CLUB THEY HAVE LEARNED  
THAT NO MATTER WHAT HAPPENS TO  
THEM IT WILL NOT BE THE END OF THEIR  
EXISTENCE



THEIR AT THE SOURCE, THEY WILL BECOME  
WILDER ONCE MORE. A NEW FORM WILL  
DEFINE A NEW PURPOSE THAT OTHERS MAY  
PUT TO GOOD USE.



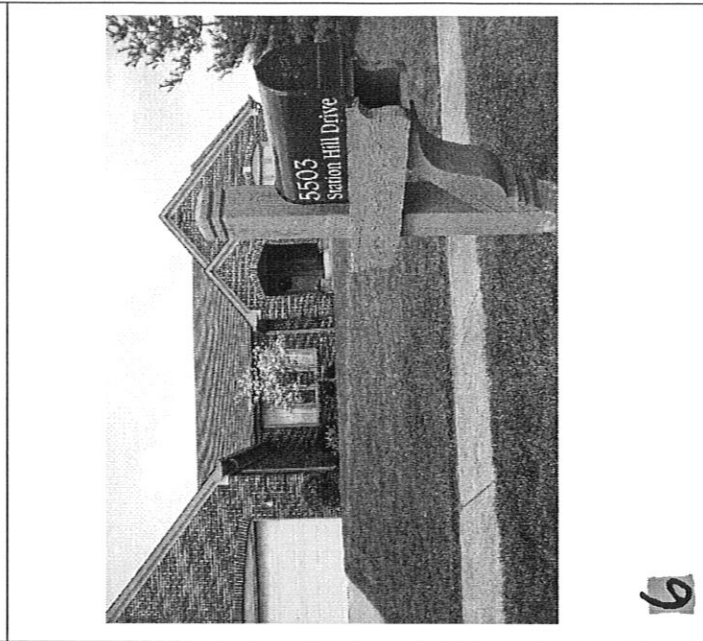
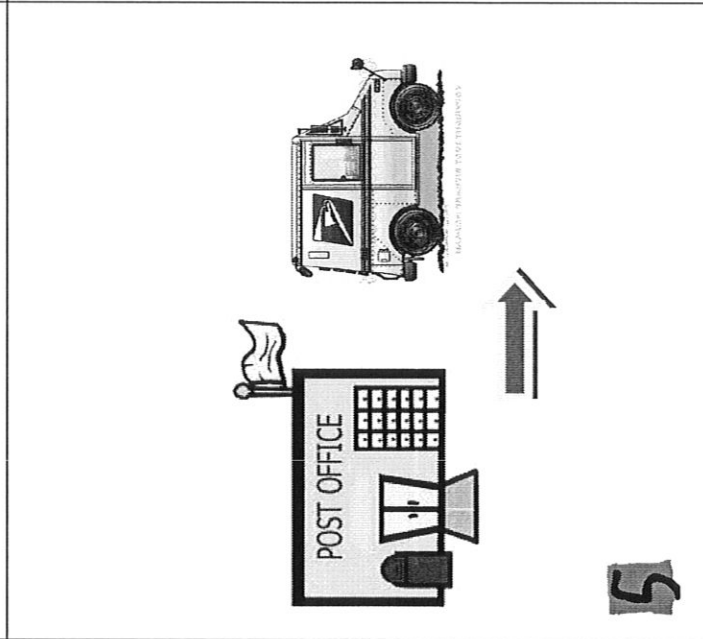
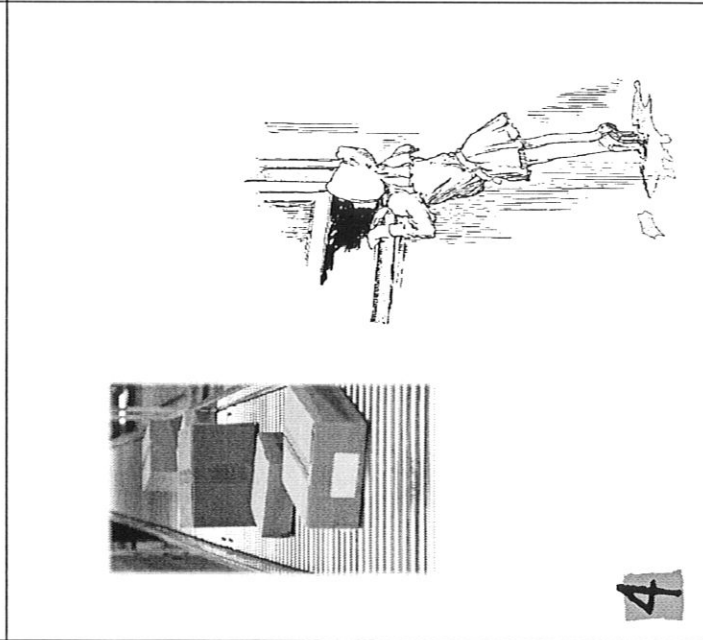
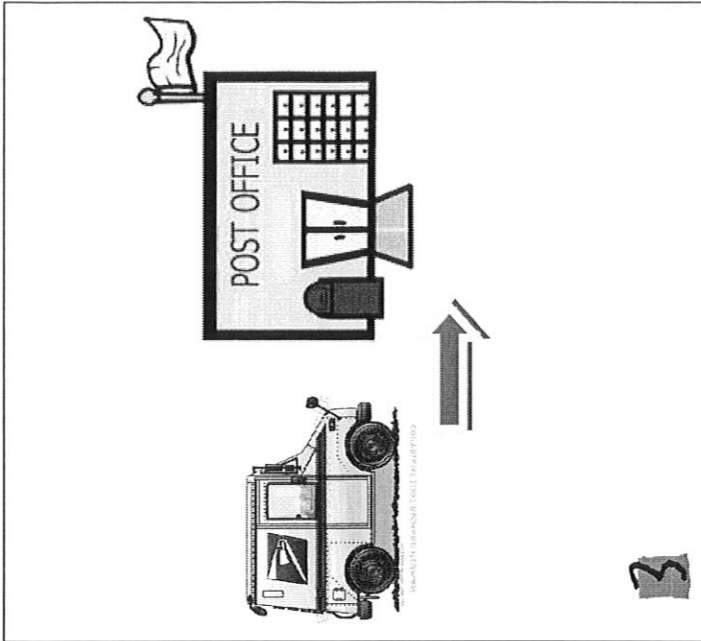
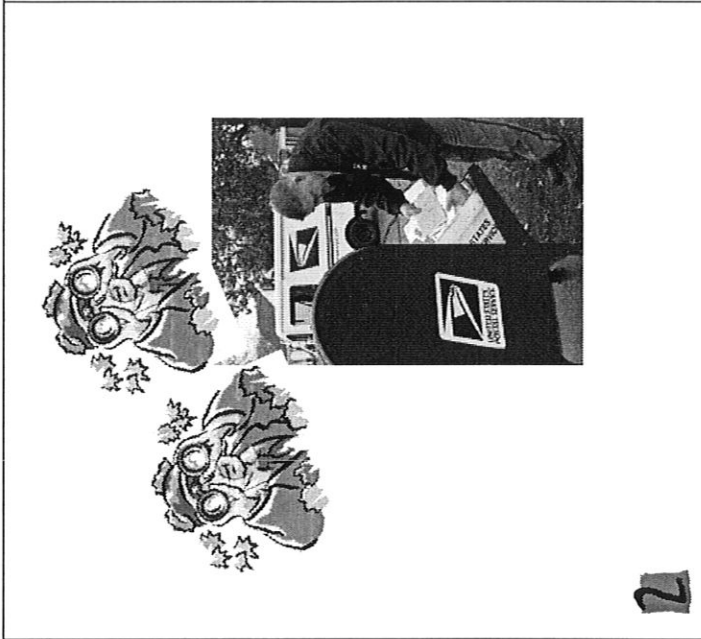
THEY MAY HAVE FULFILLED THE PURPOSE OF THEIR  
CURRENT FORM, BUT THE PURPOSE OF  
THEIR ELEMENTAL COMPOSITION SHALL LAST  
FOR EVER



REUNITED AT LAST THE THREE FRIENDS  
ONCE AGAIN ENJOY SOME GOOD LAUGHS.







## Panel 1:

Peter is standing in front of a mail drop box looking very worried and wondering whether or not he should drop the letter which he is holding in his hand. His friend Connie sees him and walks up to ask him what the matter is. Peter explains that he has something very important that he needs to have delivered, but he's afraid that his letter may get lost if he lets it out of his sight. Connie tries to reassure him and explains that his letter won't just vanish. She then explains the principle of the conservation of mass.

$$0 = \frac{\partial}{\partial x} \int \rho dV + \int \rho V \cdot n dA$$

- The post office can't be hanging on to the mail it takes in or it would soon be overflowing, so the temporal part of the continuity equations is zero.

$$0 = \int \rho V \cdot n dA$$

- Since the post office isn't keeping any of the mail then anything that goes into the post office has got to come out.
- Assuming the post office doesn't compact the mail they take in then the density of the mail is constant, so the equation becomes:

$$0 = \Sigma Q_{out} - \Sigma Q_{in}$$

(the amount of mail coming into the post office on the mail trucks is equal to the amount of mail leaving on the mail trucks).

Peter is finally convinced to drop his letter in the mail box.

## Panel 2:

Peter is still very worried about what is going to happen to his letter and wants to wait to see what will happen to it when the mail truck comes. He and Connie hide behind a bush and wait for the mail to be picked up. Eventually the mail truck comes, and Peter sees his letter being loaded into the mail truck.

## Panel 3:

Connie takes the still concerned Peter to the post office to where they see the mail truck that picked up Peter's letter pulling in next to the other mail trucks. Connie again explains that the mail coming in on all of these trucks will "flow" through the post office and then will be loaded on the trucks again to flow out of the post office.



## Panel 4:

Peter, needing some more reassurance peers through a window and sees the mail being delivered by the trucks being loaded onto a conveyor belt. He's very excited to notice his letter among the others. Connie convinces Peter, who is feeling a little better, to go home.

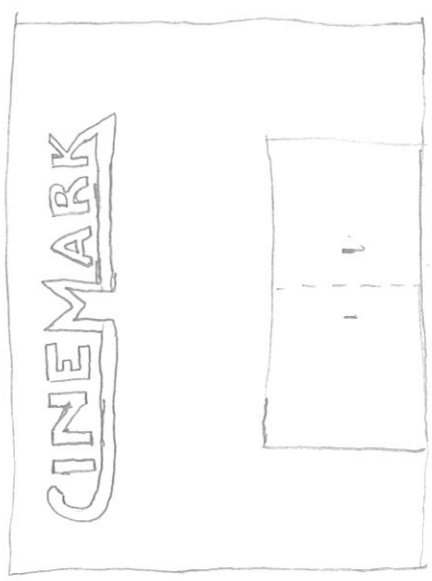
## Panel 5:

Early the next morning Peter is once again concerned for the welfare of his letter. He goes to the post office to wait for the mail to be loaded onto the trucks. As he's waiting there Connie, who suspected that he might come back, shows up to wait with him. Connie again explains that all of the mail that was taken into the post office the previous evening now has to be taken out. They see the mail being loaded into the trucks and Peter again spots his letter (obviously this is a very recognizable piece of mail, maybe it's in a bright red envelope or something). They watch as the mail trucks pull away the post office. Peter wants to follow the truck that has got his letter, but Connie convinces him not to, and invites him over to her house so she can keep an eye on him.

## Panel 6:

Peter is enjoying himself at Connie's house. They see the mail truck pull up to deliver the mail, and Peter once again becomes very nervous. Connie suggests that they go check the mail, hoping that seeing the mail being delivered at her house will help Peter have confidence that his letter made it to its destination. As Connie pulls the mail from her mail box she recognizes the letter that Peter had sent. She sighs and gives an exasperated look at the very sheepish Peter.

①



$$\frac{DB_{sys}}{Dt} = \int p dV + \int p \vec{v} \cdot \vec{n} dA$$

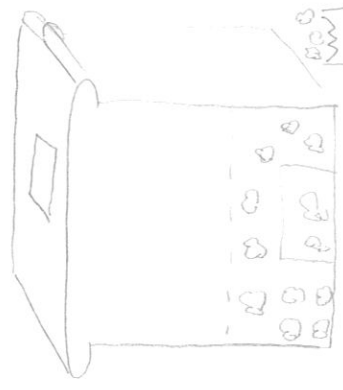
Have you ever thought that your \$6.50 an hour job at the local movie theater was merely customer service -- that there could not possibly be anything technical about it? Well, think again.

④



Stop adding kernels

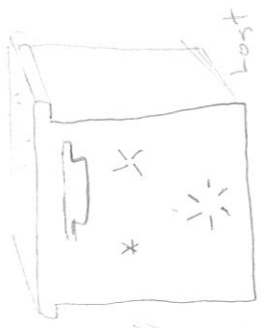
$$0 = \int p dV + Q_{out} - Q_{in}$$



Level starts to drop

②.0

$$\left( \frac{DB_{sys}}{Dt} \right) = \int p dV + \int p \vec{v} \cdot \vec{n} dA$$



0 → { } + { }  
But nothing is created or lost

②.5

$$0 = \int p dV + Q_{out} - Q_{in}$$

CLOSED Starts Empty

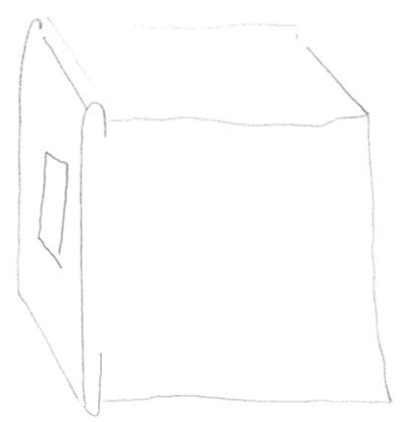
Kernels



⑤

CLOSED

$$0 = \int p dV + Q_{out} - Q_{in}$$



Empty & clean again

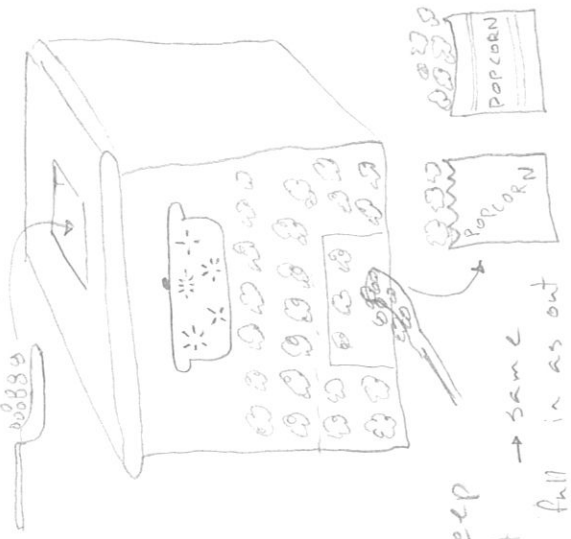
(Could even talk about cleaning out oil, etc -- more  $\int p dV + Q_{out}$ )

③

After

OPEN

$$0 = \int p dV + Q_{out} - Q_{in}$$



Keep it about full in as out

⑥

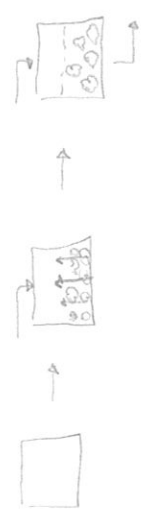
Previous

Simply

indicated highlighting.

Here we review & explain in more detail.

Same images, but with explanation rather than story telling.



→ → → \$\$\$? Yes, but too.

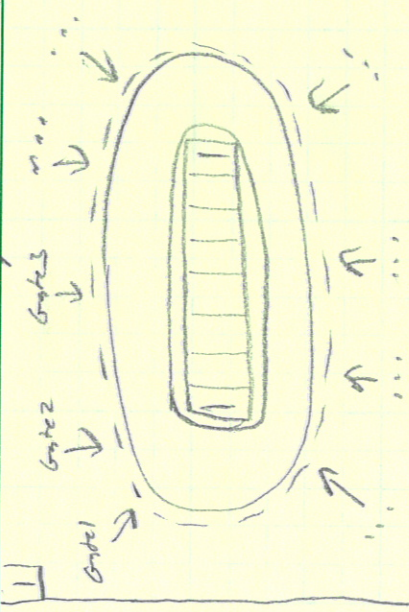


Joseph Clark  
David Palmer  
Miguel Medina

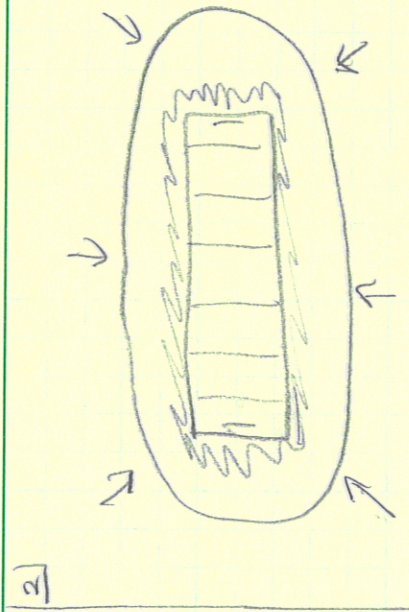
Project  
Storyboard

COMET

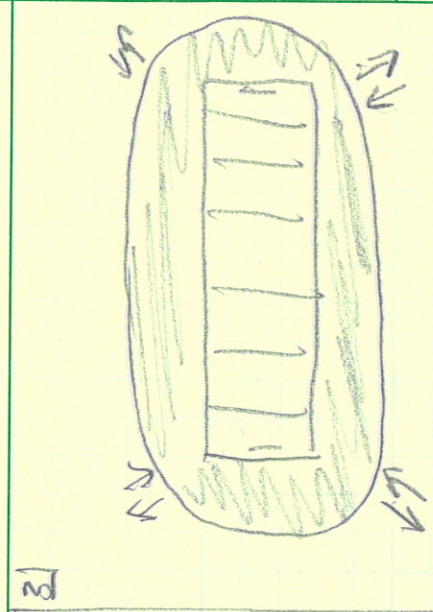
3-0235 — 50 SHEETS — 5 SQUARES  
3-0236 — 100 SHEETS — 5 SQUARES  
3-0237 — 200 SHEETS — 5 SQUARES  
3-0137 — 200 SHEETS — FILLER



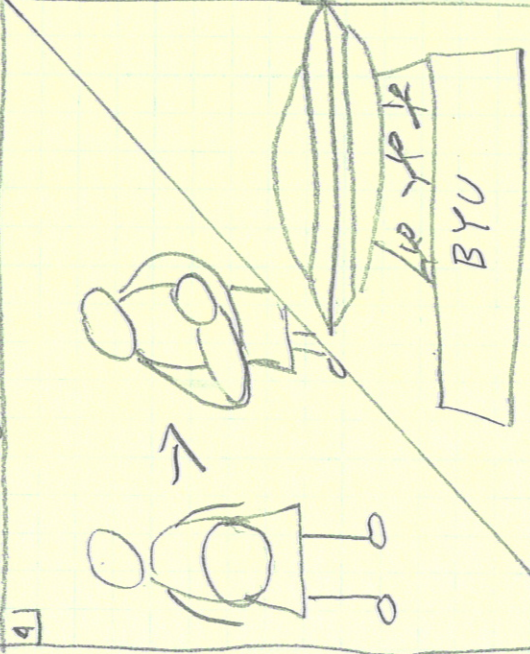
INTRO: Explain Concept. Football Stadium is the control Volume. Gates are Control Surfaces



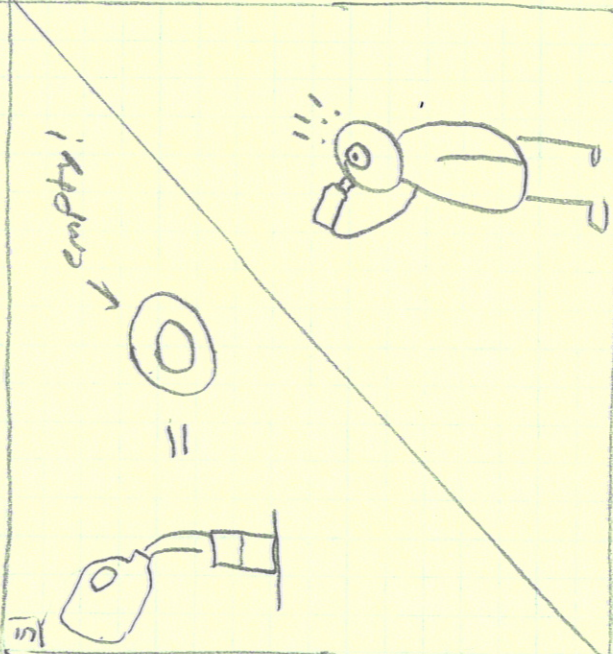
Have People fill stands  
- Unsteady flow



Stadium full, one person enters for every one person exits  
- Steady flow



W/O Conservation of mass, Mass could be added to or taken from system w/o being accounted for - This is like all of the pregnant women in the stadium giving birth to twins, or aliens abducting the U of U fans!



This could be compared to filling a glass w/ Juice and it being empty before you drink it, or drinking out of a bottle that never runs dry.

$$\frac{dm}{dt} = \frac{d}{dt} \int_V \rho dV + \int_V \rho \vec{v} \cdot \vec{n} dA = 0$$

Change in mass with respect to t

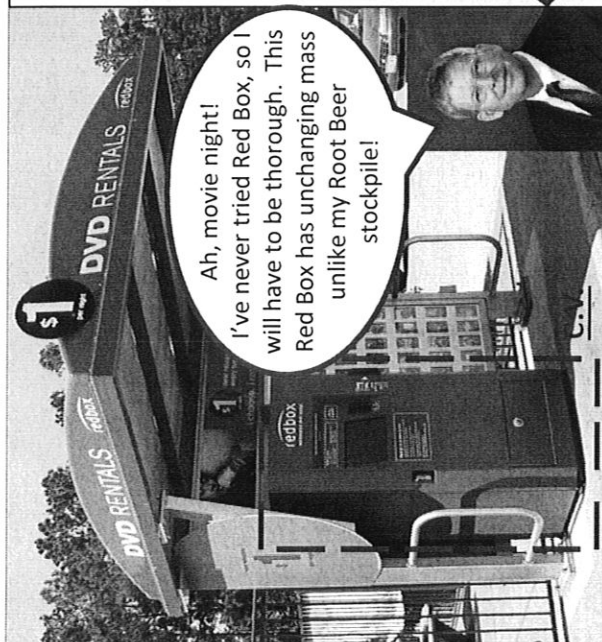
In flow vs. Out flow

Change of mass in the system over time = 0 because Mass cannot be created or destroyed!

Explanation of equation.

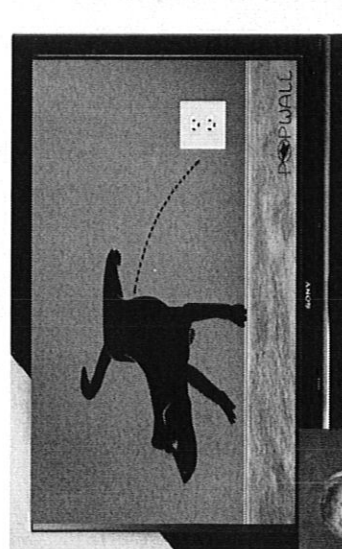
END



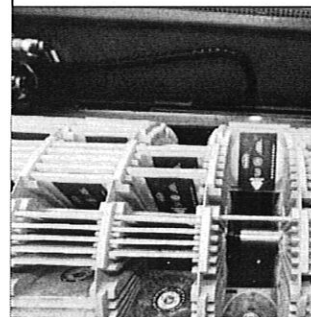


Ah, movie night!  
I've never tried Red Box, so I will have to be thorough. This Red Box has unchanging mass unlike my Root Beer stockpile!

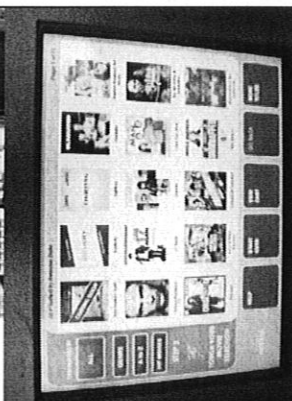
$$\frac{DB_{sys}}{Dt} = \frac{\partial}{\partial t} \int_{CV} \rho b dV + \int_{CS} \rho b \vec{V} \cdot \hat{n} dA$$



Great movie so far. We've got some good laminar flow happening.

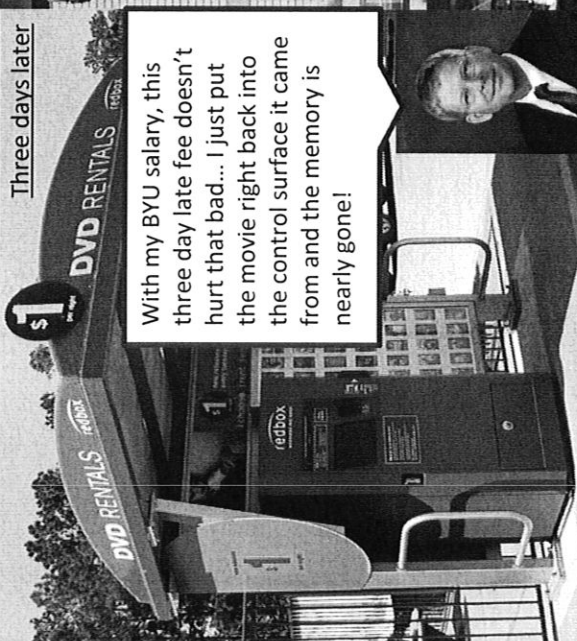


With so many options, I'll make a sweeping assumption that this system has a constant density. I just wish it had my favorite fluids movies in stock.



So many choices made possible by this thermal recognition screen.

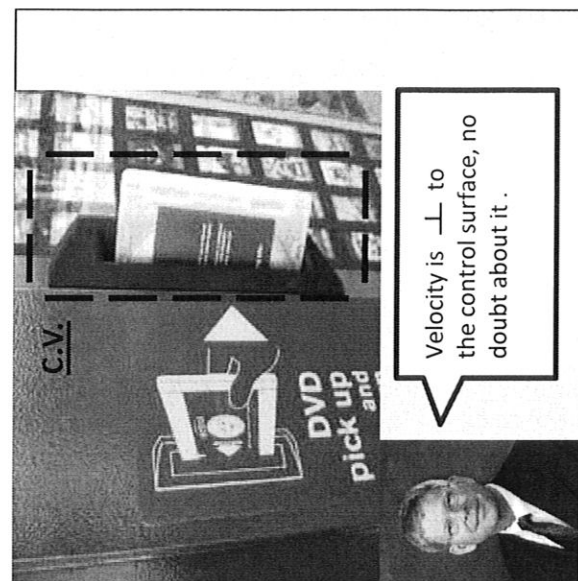
$$\frac{DB_{sys}}{Dt} = \frac{\partial}{\partial t} \int_{CV} \rho b dV + \int_{CS} \rho b \vec{V} \cdot \hat{n} dA$$



Three days later

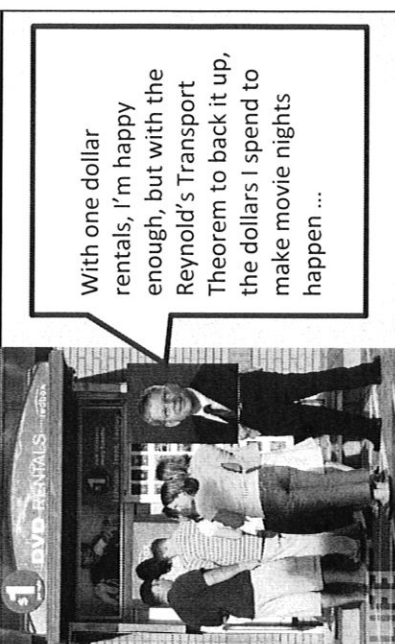
With my BYU salary, this three day late fee doesn't hurt that bad... I just put the movie right back into the control surface it came from and the memory is nearly gone!

$$\frac{DB_{sys}}{Dt} = \frac{\partial}{\partial t} \int_{CV} \rho b dV + \int_{CS} \rho b \vec{V} \cdot \hat{n} dA$$



Velocity is  $\perp$  to the control surface, no doubt about it.

$$\frac{DB_{sys}}{Dt} = \frac{\partial}{\partial t} \int_{CV} \rho b dV + \int_{CS} \rho b \vec{V} \cdot \hat{n} dA$$



With one dollar rentals, I'm happy enough, but with the Reynold's Transport Theorem to back it up, the dollars I spend to make movie nights happen ...



...are going to make someone very wealthy!

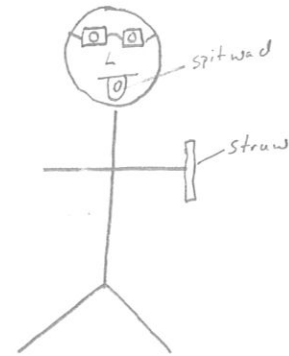
1] Conservation of mass

Spit wad

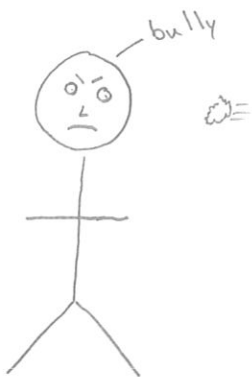


$$0 = \frac{d}{dt} \int_{cv} \rho dV + \int_{cs} \rho \vec{V} \cdot \vec{n} dA$$

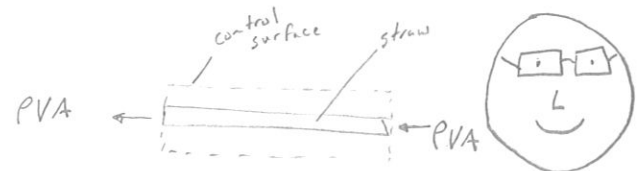
2] Little nerd Loads the straw with spit wad.



3] Steady flow



$$0 = \frac{d}{dt} \int_{cv} \rho dV + \int_{cs} \rho \vec{V} \cdot \vec{n} dA$$

4] Constant velocity  
Velocity perpendicular to control surface

$$0 = \sum \rho_{out} V_{out} A_{out} - \sum \rho_{in} V_{in} A_{in}$$

5] Density of Air is unchanged at instant  
the spit wad is shot

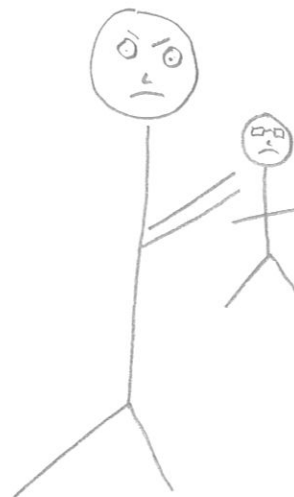
$$\rho V A = \rho V A$$

$$0 = V_{out} A_{out} - V_{in} A_{in}$$

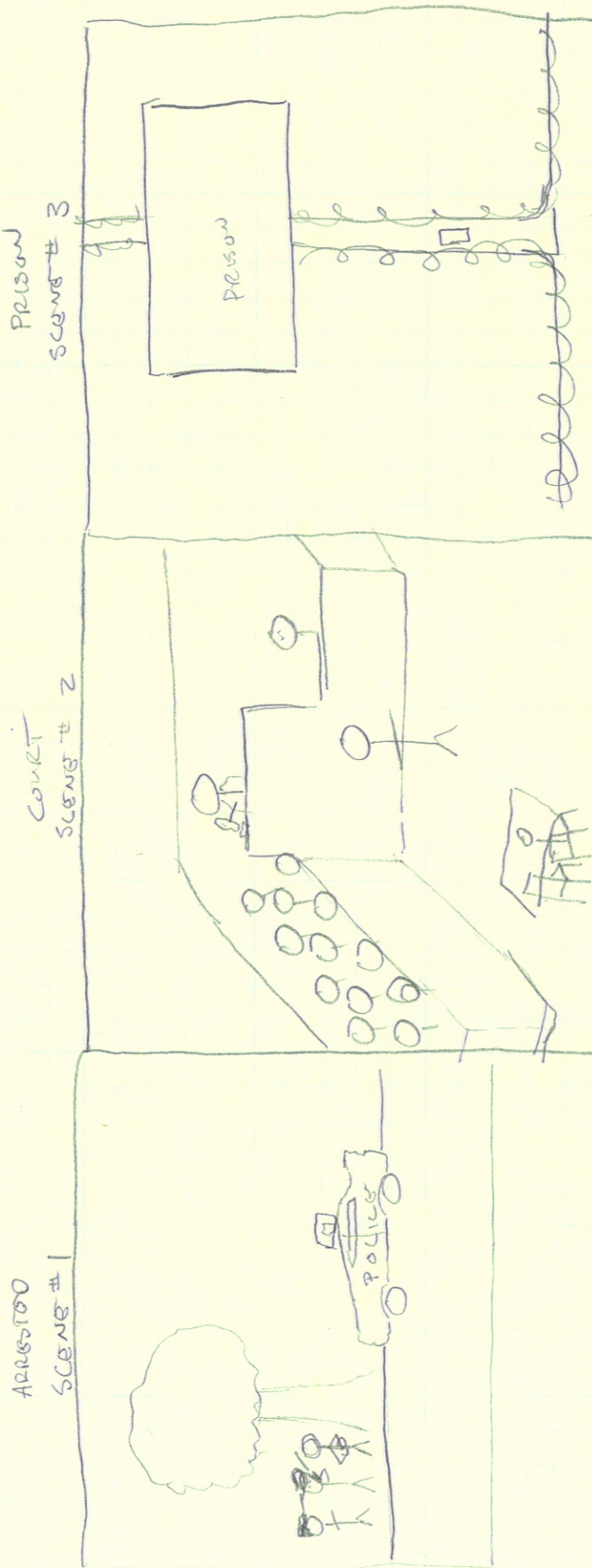
or

$$0 = Q_{out} - Q_{in}$$

6] Nerd gets bent up by bully







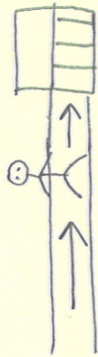
IN THE FIRST SCENE A PERSON IS  
ARRESTED FOR COMMITTING A CRIME  
(COULD BE ILUSTRATED). THIS  
SCENE AND THE NEXT ARE MAINLY  
TO SET UP THE STORY NOT EXPLAIN  
THE CONSERVATION OF MASS PRINCIPLE.

THE CRIMINAL IS TRIED IN COURT  
i. FOUND GUILTY. A PRISON  
SENTENCE IS GIVEN AND HE IS  
TAKEN AWAY.

THIS SCENE IS AN OVERHEAD VIEW  
OF THE CRIMINAL BEING BROUGHT  
TO PRISON. THE PRISON IS THE  
CONTROL SURFACE. THE ROAD LEADING  
TO THE PRISON DOOR IS  $\perp$  TO THE CS.  
FULFILLING ONE OF THE ASSUMPTIONS TO  
SIMPLIFY THE CONSERVATION OF MASS  
EQUATION.



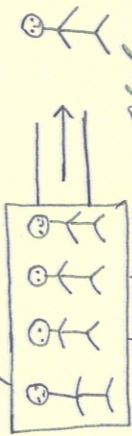
$$0 = \int_{CS} \rho \vec{V} \cdot \vec{n} dA$$



$\vec{V} \perp CS$ , CS is prison gate

$$0 = V \int_{CS} \rho dA$$

control volume

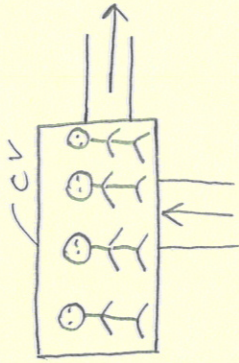


old criminal

(new criminal)

$\rho \dot{V}_{out} = \rho \dot{V}_{in}$  (Assuming same  $\rho$ )

$$\dot{m}_{out} = \dot{m}_{in}$$



The criminal are entering and leaving the prison. Still the mass of controlled volume is not changing.

$$\dot{Q}_{out} = \dot{Q}_{in}$$



The conservation of mass eg. can be used to track the change in a system of a particular variable over time.

$$\frac{DB_{sys}}{Dt} = \frac{\partial}{\partial t} \int \rho dV + \int \rho \vec{v} \cdot \vec{n} dA$$

To illustrate this, let's look at the change in hospital occupancy (living patients)

Breaking down the equation we see:

$$\frac{DB_{sys}}{Dt} = \frac{\partial}{\partial t} \int \rho dV + \int \rho \vec{v} \cdot \vec{n} dA$$

↑  
change in occupancy in the hospital over time

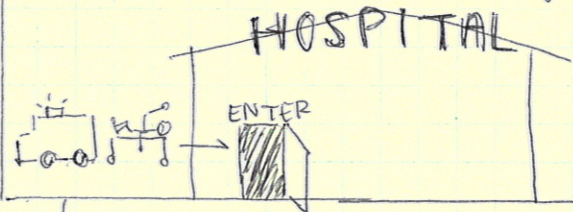
↑  
rate of people coming & going

↑  
change of patients inside the hospital, corresponding to births & deaths

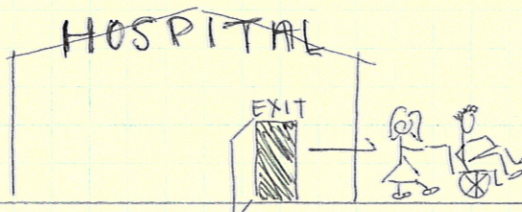
Say in a given day the # of births equals the # of deaths. We can say that the # of occupants in the hospital is steady & the first term goes away.



In that same day there were 3 patients admitted every hour. This goes under the second term, because it deals with the entrance of the system we are looking at.



Every hour there are also 2 patients released. This goes under the second term as well because it also deals with a boundary of the system.



$$\frac{D_{patients}}{D_{time}} = \frac{\partial}{\partial t} \int \rho dV + Q_{released} - Q_{admitted}$$

So the change in patients in the hospital over this particular day is completely dependent on the rate of patients coming out - those coming in.



# THAT ONE TEAM: PAUL DYRENG, TONY MELCHER, BRENT MCCREA

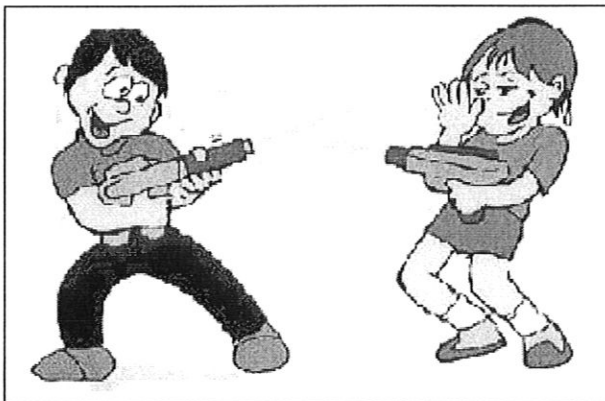


Two kids begin with an argument about  
Which super soaker is better.



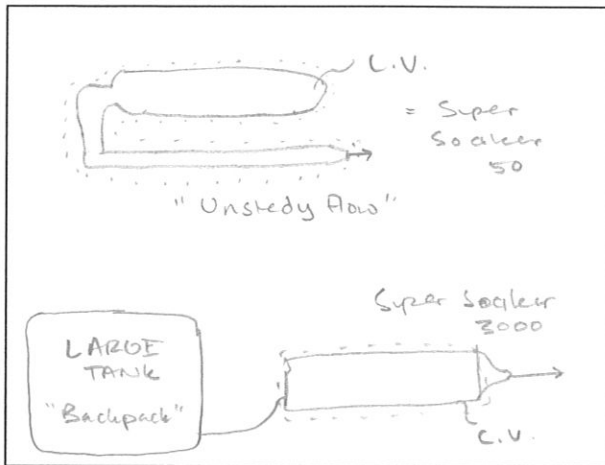
We have the super soaker 3000 with "large  
Tank" Representing steady flow

We have a super soaker 50 with unsteady  
flow.

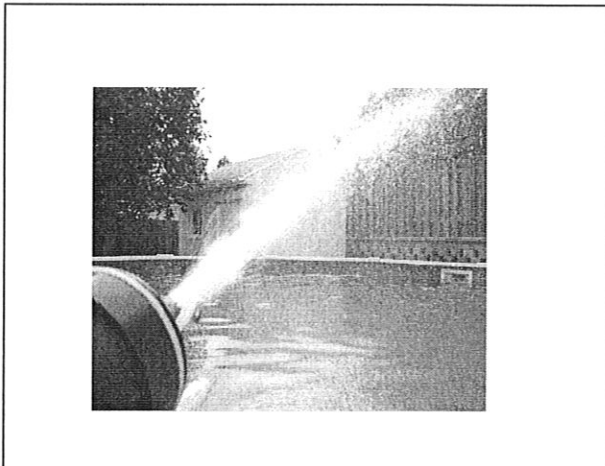


The two kids begin their water fight at this  
point we pause the film to take a look at the

Control volume of each super soaker.



Here we have the two super soakers. We teach control volume from the super soaker inside



Flowrate of the two supersoakers will then be discussed by comparing velocities and areas.



By adjusting the area, the smaller super soaker can pack a serious punch due to velocity... without Changing the amount of mass.

# JERRY & CLYDE!

The Conservation of Mass Equation

...THERE WAS TROUBLE BREWING AT THE APARTMENT...

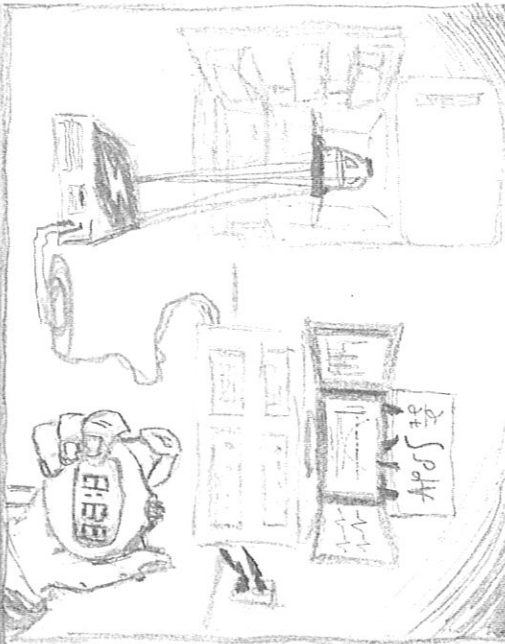


There is something wrong with our fridge, Clyde! I always find less milk in my jug than I left! We need to get a new fridge that won't steal all my milk!

Nothing wrong with the fridge. Look at this "FLUP EQUATION" called "THE CONSERVATION OF MASS EQUATION". It is very complicated, with two separate integrals, partials, and vectors. It proves that some of your milk will just disappear! But I wouldn't expect you to understand.

AND WHAT DID YOU FIND?

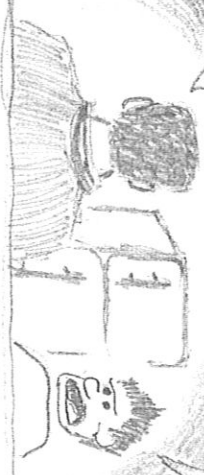
The second test dealt with change over time. Two precision measurements of your milk were done at separate times, each involving high-accuracy laser scanners, two multi-functional digital scales, a super computer, and an ordinary stop watch.



Unconvinced by Clyde, Jerry calls in for professional help. When the BYU agent arrives, Jerry explains his problem.

So, what's wrong with the fridge?

Your room mate is correct in that this problem deals with the conservation of mass equation, but his conclusion is completely wrong. The conservation of mass equation must always equal zero because mass can never be neither created nor destroyed. I will have to conduct two scientific tests, one for each integral of the equation, to determine the cause of your disappearing milk...



Unfortunately I had forgotten to remove the electrified handles...

Why? What happened?

I found that there was no change in your milk in either test, meaning that there is no problem with your fridge. But because the conservation of mass must always be equal to zero, one last test was required, involving infra-red security cameras, tap wires and electronic check points with self-locking doors...



The first test dealt with special change. I set the control volume at the fridge itself and made certain that no change in volume was occurring. This was done by the use of steel bands, welded around the frame, and sealed their around the doors and a set of two weight scales on top. The scale was connected to the handles with purely new style, high-power X-rays provided real-time analysis of the exact quantity of milk in your jug, proving that no milk was entering or leaving the control volume.



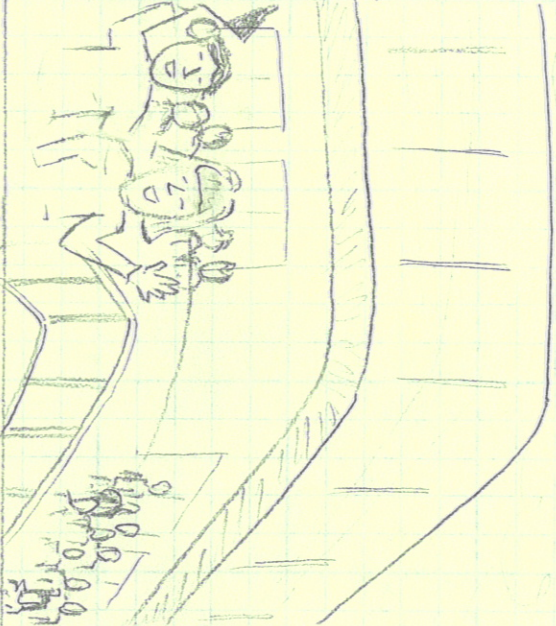
Let's just say that your roommate Clyde was "shocked" when I was able to prove what I had suspected all along: he had been stealing your milk late at night and teaching you the conservation of mass equation wrote in code to cover his tracks! So, kids, always remember this: the sum of both integrals found in the conservation of mass equation, both the special and the temporal must always equal up to zero!



END



Basketball game ends at Marroth Center. Crowds exit.



GAASP! Flow area is reduced. Crowds must pass through narrower walkway. ( $A_2 < A_1$ )



Crowds approach walkway. Walkway is finite width (Flow area). Steady flow, e.g., 1000 people / minute.



Pushed from behind, fans in front

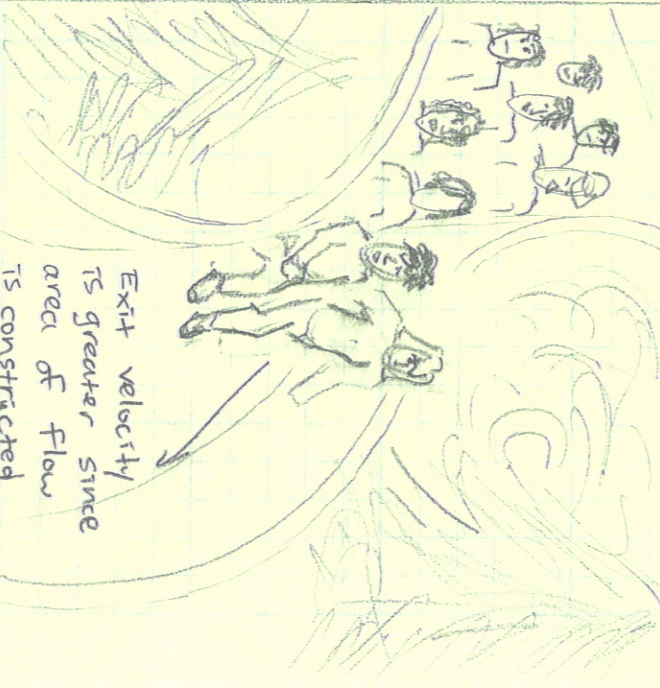
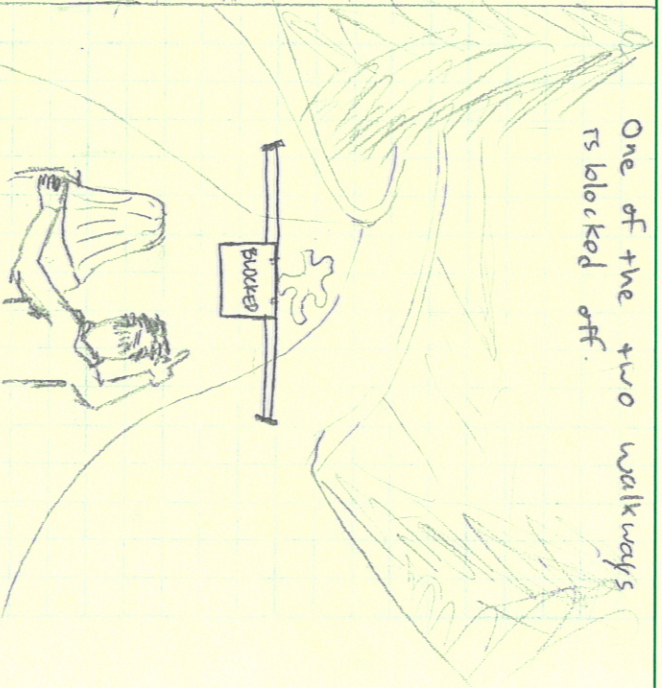
Must accelerate to walkway exit to

$$V_2 > V_1$$

COMET

maintain constant flow rate ( $Q$ ).

One of the two walkways is blocked off.



Exit velocity is greater since area of flow is constricted.

$$V_2 > V_1, A_2 < A_1$$

$$Q_2 = Q_1$$

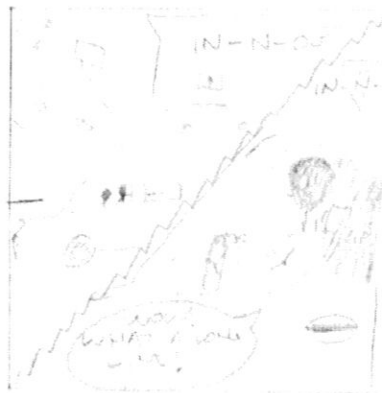
$$V_2 A_2 = V_1 A_1$$

3-0235 50 SHEETS  
3-0236 100 SHEETS  
3-0237 200 SHEETS  
3-0137 200 SHEETS  
FILLER  
5 SQUARES  
5 SQUARES  
5 SQUARES



# CONSERVATION OF MASS: IN-N-OUT

## IN-N-OUT BURGER



Two people driving to in-n-out not long after it opened for the first time. They see the line and comment about how the line is a always full of cars (steady flow). conversation goes something like this:

- 1) "Hey man there's in-n-out, we should go there!"
- 2) "Yeah they make great food but the line is always crazy long"
- 1) "That's alright, we've got plenty of time and it'll be worth the wait."
- 2) "Yeah, you're right let's do it. I can't get over how busy it always is though. The other day I was watching the line while I was standing out here waiting for a ride. I counted up the cars, ate a cookie, then I counted them again and it was exactly the same."

Waiting in line previous to ordering food (uniform or constant velocity)

- 1) "Well your right about the slow line. We just keep moving about five feet every 60 seconds, seems pretty constant"
- 2) "We'll get there eventually though, and besides at least it's slow for everyone and not just us."



At the ordering kiosk, just after ordering (velocity is normal to control surface, the car is now is passing into the control volume)

- 2) "Alright sweet, now it's just straight ahead from here to the food. I'm so excited"
- 1) "Yeah and now the wait's not so bad because we're like "in" now that we've passed the ordering station. Once we're in at least we know that our food is on the way."

"Thanks for coming to In-n-out here's your food" "Thank you"

In this frame the In-n-out worker will deliver the food to the customers in the car. As the food comes out of the window we notice that the food is delivered perpendicular to the window which is the control surface. In regards to the formula this means that the dot product of  $N$  and  $V$  is equal to the magnitude of  $N$  times  $V$  times the Cosine of the angle between the two, which is just the magnitude to  $V$ .



"This looks so good, let get out of here" "I'm glad we came."

The customers are leaving the drive through lane. Again the cars leaving are perpendicular to the control surface. And because this is steady flow the mass out is equal to the mass in. So even though we have two control surfaces coming in, all of the mass is leaving through this control surface.

Summary: Steady flow- because there are always cars going through the drive through

Constant or uniform velocity- because the cars are continuously rolling forward as other cars leave

Velocity is normal to the control surface- as the cars come in and out of the control volume they do so perpendicular to the control surface

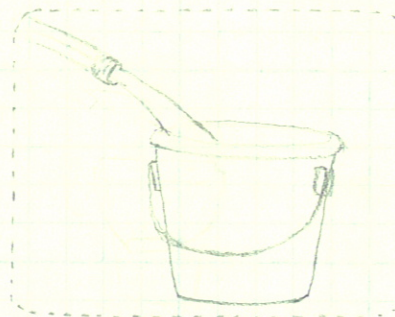
1

## Conservation of Mass

$$\frac{d}{dt} \int_{cv} \rho dV + \int \rho \vec{V} \cdot \vec{n} dA = 0$$

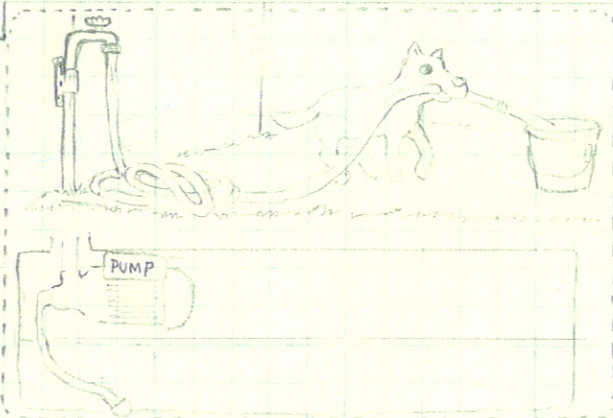
why does the conservation of mass equation equal zero?

2



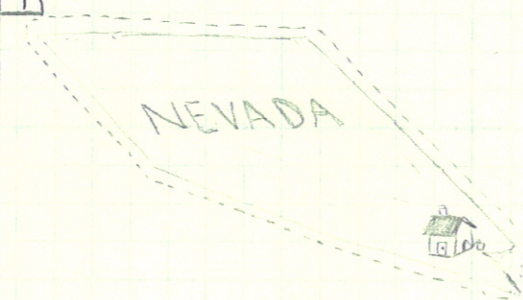
look at this system and how the mass changes with respect to time. So how the equation still equal zero? let take a larger control volume

3



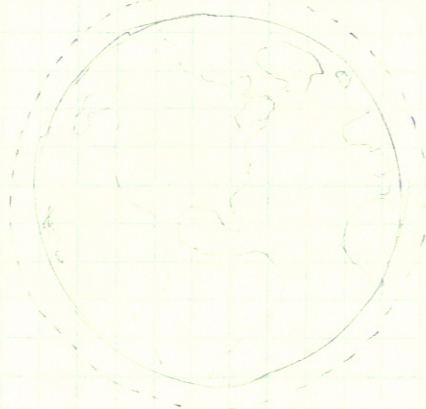
with a control volume that encompass the previous, the water that is goes into bucket comes from the well, but the mass changes due water seeping out or in the well, the dog coming or leave mass still changes with time but it is smaller and different.

4



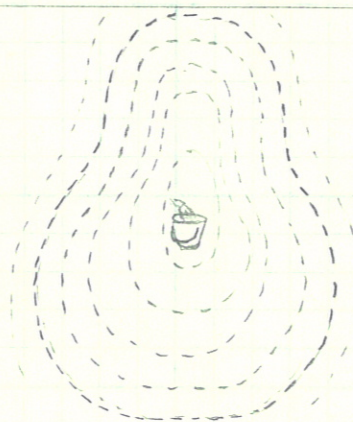
Pick a control volume that contains that one like the state of Nevada. once again mass is changing no so much with water seeping in and out of that well but more with addicted gamblers and travelers. So pick a bigger control volume.

5



continues over and over again, soon the amounts of mass changing in system decreases or changes. If we were to stack this up it would look alot those stacking Russian dolls.

6



There is always a larger control volume that will encompass the previous one so you think of that  $\frac{DB_{sys}}{dt} = 0$ . galactically and locally.



Jake Grow  
Jaron Knighton  
Kassidy Shumway

1

## Conservation of Mass

$$\sum \dot{M}_{in} - \sum \dot{M}_{out} = \Delta M_{sys}$$

2

Overview: Family walks to waterslide park. They look around and get a general picture of waterslide with inflows and outflows. The rain clouds can be seen in the distance. The price for the park is per pound, so the family is weighed so we know how much mass they are bringing in.

3

Inflows: Water coming down slide, people (all of the happy family), tubes, child urine, and rain.

4

Outflows: Turns sunny and there is evaporation, people getting out of pool, water pumped up to top of slide from pool.

5

Stays: Water, some tubes, and a sad child

6

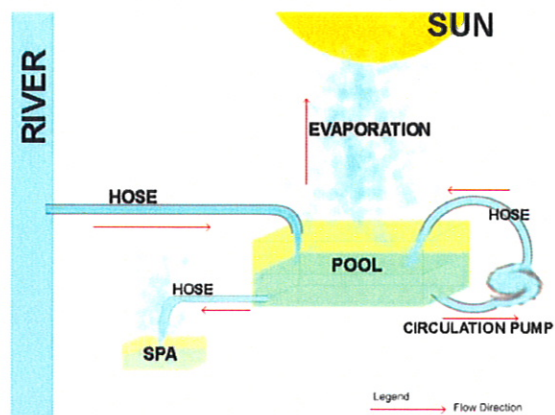
Recap and more in-depth explanation of the conservation of mass equation. The control volume is shown to be the pool at the end of the slides. The mass in the pool has to do with what flows in, outflows and what is left behind.

1

# Conservation of Mass

$$\sum \dot{M}_{in} - \sum \dot{M}_{out} = \Delta M_{sys}$$

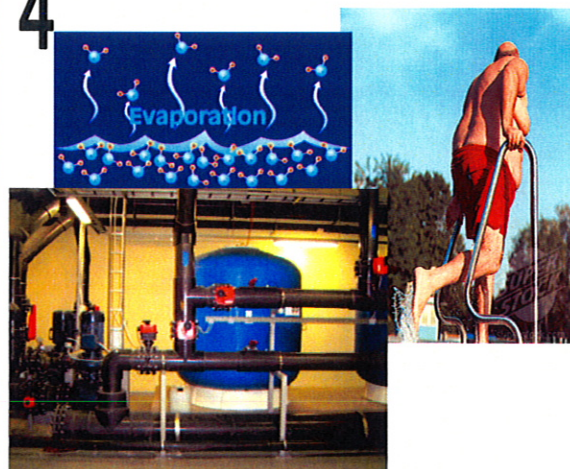
2



3



4



5



6

